(or, Deadlock-free sessions
with failure in Rust)

by Wen Kokke



A TALE OF FOUR EXAMPLES

```
(by Fowler et al.)
```

```
Looks like this:
```

```
let s = fork(\lambda(s : !1. End)).let s = send((), s)close(s))let ((), s) = recv(s)close(s)
```

(by me)

```
Looks like this:
```

```
let s = fork!(move |s: Send<(), End>| {
    let s = send((), s)?;
    close(s)
});
let ((), s) = recv(s)?;
close(s)
```

I KNOW, THE FONTS ARE VERY DIFFERENT

ROADMAP

- » talk about Exceptional GV
- » talk about Rusty Variation
- » what are the differences?
- » what are the similarities?



Let's see how our example EGV program executes!

```
egin{aligned} & \mathbf{let} \; s = \mathbf{fork}(\lambda(s: !\mathbf{1}. \operatorname{End}). \ & \mathbf{let} \; s = \mathbf{send}((), s) \ & \mathbf{close}(s) \ & ) \ & \mathbf{let} \; ((), s) = \mathbf{recv}(s) \ & \mathbf{close}(s) \ & \mathbf{close}(s) \end{aligned}
```

We mark the main thread with a • Next we evaluate the fork instruction

Let's see how our example EGV program executes!

$$u a)(
u b) \left(egin{array}{cl} \mathbf{let} \ s = a \ \mathbf{let} \ ((), s) = \mathbf{recv}(s) \ \mathbf{close}(s) \end{array}
ight) & \parallel \ \circ \left(egin{array}{cl} \mathbf{let} \ s = \mathbf{send}((), b) \ \mathbf{close}(s) \end{array}
ight) & \parallel \ a(\epsilon) {\leftrightarrow} b(\epsilon) \end{array}
ight)$$

This forks off the process and allocates a buffer Next we evaluate the let binding

Let's see how our example EGV program executes!

$$(
u a)(
u b) \left(egin{array}{cl} egin{array}{cl} egin{$$

The receive instruction blocks on the empty buffer Next we evaluate the send instruction

Let's see how our example EGV program executes!

$$(
u a)(
u b) \left(egin{array}{cl} egin{array}{cl} egin{$$

This moves the value to the buffer Next we evaluate the let binding

Let's see how our example EGV program executes!

$$(
u a)(
u b) \left(egin{array}{close(s)} egin{array}{close(s)} & \| & \ close(b) \ & \circ ({f close(b)}) & \| & \ & a((),\epsilon){\color{red} \leftarrow} b(\epsilon) \end{array}
ight)$$

The close instruction blocks (it is synchronous) Next we evaluate the receive instruction

Let's see how our example EGV program executes!

$$u a)(
u b) \left(egin{array}{close(s)} egin{array}{close(s) \ \circ ({f close}(b) \ a(\epsilon) {
ightarrow b}(\epsilon) \end{array}
ight) & \parallel \ \end{array}
ight.$$

This moves the value to the main thread Next we evaluate the let binding

Let's see how our example EGV program executes!

The close instructions are no longer blocked

(The buffer is empty and there is a close instruction waiting on either side)

Next we evaluate the close instructions

Let's see how our example EGV program executes!

•()

Fin

What about our Rust program?

```
let s = fork!(move |s: Send<(), End>| {
    let s = send((), s)?;
    close(s)
});
let ((), s) = recv(s)?;
close(s)
```

```
let s = fork!(move |s: Send<(), End>| {
    let s = send((), s)?;
    close(s)
});
let ((), s) = recv(s)?;
close(s)
```

```
let (s, here) = <Send<(), End> as Session>::new();
std::thread::spawn(move || {
    let r = (move || -> Result<_, Box<Error>> {
        let s = send((), s)?;
        close(s)
    })();
    match r {
        Ok() => (),
        Err(e) => panic!("{}", e.description()),
    }
}]:
let s = here
```

```
let (b, a) = <Send<(), End> as Session>::new();
std::thread::spawn(move || {
    let r = (move || -> Result< , Box<Error>> {
        let b = send((), b)?;
        close(b)
    })();
    match r {
        Ok(_) => (),
        Err(e) => panic!("{}", e.description()),
    }
});
```

```
let (b, a) = <Send<(), End> as Session>::new();
```

```
std::thread::spawn(move | {
}]:
```

```
let r = (move || -> Result< , Box<Error>> {
    let b = send((), b)?;
    close(b)
})();
```

```
match r {
    Ok(_) => (),
    Err(e) => panic!("{}", e.description()),
}
```

```
let b = send((), b)?;
let ((), a) = recv(a)?;
```

SOUNDS FAMILIAR?

LET'S TALK ABOUT ERRORS

```
(by Fowler et al.)
```

```
Looks like this:
```

```
let s = \mathbf{fork}(\lambda(s : !1. \text{End})).

cancel(s)

)

let ((), s) = \mathbf{recv}(s)

close(s)
```

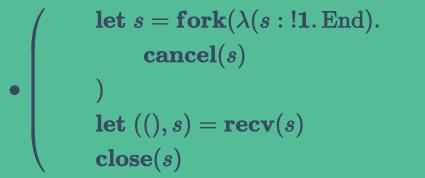
(by me)

```
Looks like this:
```

```
let s = fork!(move |s: Send<(), End>| {
    cancel(s)
});
let ((), s) = recv(s)?;
close(s)
```

I KNOW, THE FONTS ARE VERY DIFFERENT

Let's see how EGV handles errors!



We mark the main thread with a • Next we evaluate the fork instruction

Let's see how EGV handles errors!

$$(
u a)(
u b) \left(egin{array}{cl} \mathbf{et} s = a \ \mathbf{let} ((), s) = \mathbf{recv}(s) \ \mathbf{close}(s) \end{array}
ight) \parallel \ \mathbf{close}(s) \circ (\mathbf{cancel}(b)) \parallel \ a(\epsilon) {\mbox{\ensuremath{\leftarrow}\mbox{\ensuremath{\leftarrow}\mbox{\ensuremath{\leftarrow}\mbox{\ensuremath{\cdot}\mbo$$

This forks off the process and allocates a buffer Next we evaluate the let binding

Let's see how EGV handles errors!

$$(
u a)(
u b) \left(egin{array}{cl} egin{array}{cl} egin{$$

The receive instruction blocks on the empty buffer Next we evaluate the cancel instruction

Let's see how EGV handles errors!

This cancels the session and creates a zapper thread Next we evaluate the receive instruction

Let's see how EGV handles errors!

$$(
ua)(
ub) \left(egin{array}{close(s)} egin{array}{close(s)} & \| & \| \ & a(\epsilon) & & b(\epsilon) & \| \ &
eq b & \| \ &
eq a & \| \end{array}
ight)$$

Receiving on a channel raises an exception if the other endpoint is cancelled

Let's see how EGV handles errors!

An uncaught exception turns into halt Next we garbage collect the buffer

Let's see how EGV handles errors!

• halt

Fin

What about the Rust library?

```
let s = fork!(move |s: Send<(), End>| {
    cancel(s)
});
let ((), s) = recv(s)?;
close(s)
```

RUSTY VARIATION

For that, let's look at how cancel is implemented:

fn cancel<T>(x: T) -> Result<(), Box<Error>> { Ok(()) }

Wait, what happened to x?

It went out of scope!

RUSTY VARIATION

What happens when a channel x leaves scope unused?

- » destructor is called
- » values in buffer are deallocated
- » destructors for values in buffer are called
- » buffer is marked as DISCONNECTED
- » calling recv on DISCONNECTED buffer returns Err

SOUNDS FAMILIAR?

WHAT ARE THE DIFFERENCES?

» <u>try/catch</u> vs. <u>error monad</u>

(using the "try Las x in Notherwise M" instruction)

» <u>explicit close</u> vs. <u>implicit close</u>

fn close(s: End) -> Result<(), Box<Error>> {
 Ok(()) // `End` doesn't have a buffer
}

» explicit cancellation vs. implicit cancellation
(what happens if we forget to complete a session?)

WHAT ARE THE DIFFERENCES?

» <u>simply-typed linear lambda calculus</u> vs. <u>Rust</u>

this means we have:

- » <u>no recursion</u> vs. <u>general recursion</u>
- » <u>lock freedom</u> vs. <u>deadlock freedom</u>
- » etc.

HOW CAN WE GET DEADLOCKS IN RUSTY VARIATION?

» by using mem::forget

```
let s = fork!(move |s: Send<(), End>| {
    mem::forget(s);
    Ok(())
});
let ((), s) = recv(s)?;
close(s)
```

» by storing channels in manually managed memory and not cleaning up

WHAT ARE THE SIMILARITIES?

- » in theory, everything else?
- » can we prove it?

"doesn't Rust have formal semantics?" I heard so much about RustBelt!

no.

RustBelt formalises elaborated Rust and doesn't support many features we depend on.

WHAT ARE THE SIMILARITIES?

- » in theory, everything else?
- » can we prove it? no.
- » can we test it?

```
#[test]
fn ping_works() {
    assert!(|| -> Result<(), Box<Error>> {
        // ...insert example here...
     }().is_ok()); // it actually is!
```

WHAT ARE THE SIMILARITIES?

- » in theory, everything else?
- » can we prove it? no.
- » can we test it? yes.
- » can we properly test it?

TESTING RUSTY VARIATION

- (x) generate random EGV term
- () compile EGV term to Rust
- () run Rust term and log trace
- () check trace with EGV term

The following is an ad for FEAT/NEAT

by Claessen, Duregård, & Pałka

I wanna make stuff like this...

Let's not get ahead of ourselves, though...

 $\lambda(f: \mathbf{0} \multimap \mathbf{0}). \, \lambda(x: \mathbf{0}). \, f \, x$

 $\lambda(f: \mathbf{0} \multimap \mathbf{0}). \, \lambda(g: \mathbf{0} \multimap \mathbf{0}). \, \lambda(x: \mathbf{0}). \, f(g \, x)$

 $(\lambda(f: \mathbf{0} \multimap \mathbf{0}). f) \ (\lambda(x: \mathbf{0}). x)$

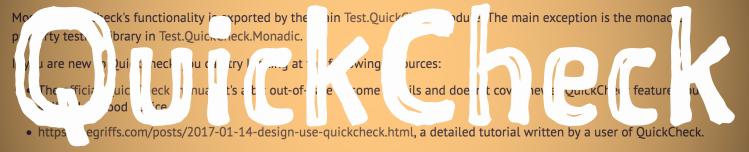
 $(\lambda(g:(\mathbf{0}\multimap\mathbf{0})\multimap(\mathbf{0}\multimap\mathbf{0})).g) \ (\lambda(f:\mathbf{0}\multimap\mathbf{0}).f)$

Let's try...

QuickCheck: Automatic testing of Haskell programs

[bsd3, library, testing] [Propose Tags]

QuickCheck is a library for random testing of program properties. The programmer provides a specification of the program, in the form of properties which functions should satisfy, and QuickCheck then tests that the properties hold in a large number of randomly generated cases. Specifications are expressed in Haskell, using combinators provided by QuickCheck. QuickCheck provides combinators to define properties, observe the distribution of test data, and define test data generators.



The quickcheck-instances companion package provides instances for types in Haskell Platform packages at the cost of additional dependencies.

[Skip to Readme]

Modules

[Index] [Quick Jump] Test

Versions

1.0, 1.1.0.0, 1.2.0.0, 1.2.0.1, 2.1, 2.1.0.1, 2.1.0.2, 2.1.0.3, 2.1.1, 2.1.1.1, 2.1.2, 2.2, 2.3, 2.3.0.1, 2.3.0.2, 2.4, 2.4.0.1, 2.4.1, 2.4.1.1, 2.4.2, 2.5, 2.5.1, 2.5.1.1, 2.6, 2.7, 2.7.1, 2.7.2, 2.7.3, 2.7.4, 2.7.5, 2.7.6, 2.8, 2.8.1,

Intermission "What is this QuickCheck you speak of?"

QuickCheck 101

You write...

import Test.QuickCheck

```
prop_revapp :: [Int] -> [Int] -> Bool
prop_revapp xs ys = reverse (xs ++ ys) == reverse ys ++ reverse xs
```

You test...

>>> quickCheck prop_revapp
+++ OK, passed 100 tests.

QuickCheck 101

instance Arbitrary a => Arbitrary [a] where arbitrary = do n <- arbitrary replicateM n arbitrary -- ^ pick arbitrary length n -- pick n things of type a

So now we all know exactly how QuickCheck works...

My good plan

- I. make some programs
- 2. run them programs
- 3. compile them to Rust
- 4. run them in Rust
- 5. see if they same

QuickCheck, some programs please?

"There is no generic arbitrary implementation included because we don't know how to make a high-quality one. If you want one, consider using the testing-feat or generic-random packages."

- xoxo QuickCheck

Fine! I'll write one myself! 😤

type Name = String

data Term = Var Name | Lam Name Term | App Term Term

```
instance Arbitrary Term where
arbitrary = oneof
  [ Var <$> arbitrary
  , Lam <$> arbitrary <*> arbitrary
  , App <$> aribtrary <*> arbitrary ]
```

Fine! I'll write one myself! 😪

Lam ">h" (Var "\EOT\NAKW")

data Term = Var Name Lam Name Term arbitrary = __neof [Var <\$> arbitrary , Lam <\$> arbitrary <*> arbitrary , App <\$> aribtrary <*> arbitrary]

Uhh, I guess I'll do some thinking... 😂

- data Z -- Z has no elements
- data S n -- S n has |n| + 1 elements = FZ -- e.g. TwoOfFour :: S (S (S (S Z))) | FS n -- TwoOfFour = FS (FS FZ)
- data Term n -- "every term is = Var n -- well-scoped, | Lam (Term (S n)) -- so no more | App (Term n) (Term n) -- nonsense."

How do I random these? 😌

```
instance Arbitrary Z where
    arbitrary = oneof [] -- a blatant lie
```

```
instance Arbitrary n => Arbitrary (S n) where
arbitrary = oneof [ pure FZ , FS <$> arbitrary ]
```

```
instance Arbitrary n => Arbitrary (Term n) where
arbitrary = oneof
  [ Var <$> arbitrary
  , Lam <$> arbitrary
  , App <$> arbitrary <*> arbitrary ]
```

How do I random these? 💬

Lam Ar (1 Lam [] (Var (IFS FZ)))

instance Arbitrary n > Arbitrary (S n) wher ib rarv = oneof [pure FZ FS <\$> arb rary] i land Ali) (0,0) > r(1) Ali (erm n) wore arbitrary = oneof [Var <\$> arbitrary , Lam <\$> arbitrary , App <\$> aribtrary <*> arbitrary]

But types?

Let's add some types...

```
data Type
   = Void
    | Type :-> Type
data Term n
   = Var n
    Lam (Term (S n))
    | App (Term n) (Term n) Type -- this is new!
check :: [Type] \rightarrow Type \rightarrow Term n \rightarrow Bool
check env a (Var n) = lookup env n == a
check env (a : -> b) (Lam t) = check (a : env) b t
check env b (App f s a) = check env (a :-> b) f \& check env a s
check _ _ _
                               = False
```

```
instance Arbitrary Type where
arbitrary = oneof
   [ pure Void
   , (:->) <$> arbitrary <*> arbitrary ]
```

```
newtype WellTyped n = WellTyped (Term n)
```

```
instance Arbitrary Type where
    arbitrary = oneof
        [ pure Void
                             , (:->) <$> arbitrary <*> arbitrary ]
newtype WellTyped n = WellTyped (Tern)
instance Arbitrary WellTyped Z where
    arbitrary = do
        a <- arbitrary -- an arbitrary type
        t <- arbitrary -- an arbitrary *closed* term
        if check [] t a then WellTyped t else arbitrary
```

instance Arbitrary Type where
arbitrary = oneof
 [pure Void
 , (:->) <\$> arbitrary <*> arbitrary]

newtype WellTyped n = WellTyped (Term n) What S going on? ... instance Arbitrary WellTyped 2 where arbitrary = do a <- arbitrary -- an arbitrary type t <- arbitrary -- an arbitrary type if check [] t a then WellTyped t else arbitrary

instance Arbitrary Type where
arbitrary = oneof
 [pure Void
 , (:->) <\$> arbitrary <*> arbitrary]

newtype WellTyped n = WellTyped (Term n) Why is nothing happening? ... instance Arbitrary WellTyped Z where arbitrary = do a <- arbitrary -- an arbitrary type t <- arbitrary -- an arbitrary type if check [] t a then WellTyped t else arbitrary

instance Arbitrary Type where
 arbitrary = oneof
 [pure Void
 , (:->) <\$> arbitrary <*> arbitrary]

```
newtype WellTyped n = YellTyped Firm for
instance Arbitrary WellTyped Firm for
arbitrary = do
a <- arbitrary -- an arbitrary type
t <- arbitrary -- an arbitrary type
if check [] t a then WellTyped t else arbitrary
```



I guess I'll do some research...

What proportion of lambda terms is typeable?

A Natural Counting of Lambda Terms

Maciej Bendkowski^{1(⊠)}, Katarzyna Grygiel¹, Pierre Lescanne², and Marek Zaionc¹

¹ Faculty of Mathematics and Computer Science, Theoretical Computer Science Department, Jagiellonian University, ul. Prof. Łojasiewicza 6, 30-348 Kraków, Poland {bendkowski,grygiel,zaionc}@tcs.uj.edu.pl ² École Normale Supérieure de Lyon, LIP (UMR 5668 CNRS ENS Lyon UCBL INRIA), University of Lyon, 46 Allée d'Italie, 69364 Lyon, France pierre.lescanne@ens-lyon.fr

Abstract. We study the sequence of numbers corresponding to λ -terms of given size in the model based on de Bruijn indices. It turns out that the sequence enumerates also two families of binary trees, i.e. black-white and ziezas-free ones. We provide a constructive proof of this fact by exhibiting

What proportion of lambda terms is strongly normalising?

"Corollary I. Asymptotically almost no $\lambda-term$ is strongly normalizing."

-- xoxo Bendkowski, Grygiel, Lescanne, and Zaionc



Can we solve this through engineering?

Generating Constrained Random Data with Uniform Distribution

Koen Claessen, Jonas Duregård, and Michał H. Pałka

Chalmers University of Technology {koen,jonas.duregard,michal.palka}@chalmers.se

Abstract. We present a technique for automatically deriving test data generators from a predicate expressed as a Boolean function. The distribution of these generators is uniform over values of a given size. To make the generation efficient we rely on laziness of the predicate, allowing us to prune the space of values quickly. In contrast, implementing test data generators by hand is labour intensive and error prone. Moreover, handwritten generators by hand is labour intensive distribution of values, risking that some values are arbitrarily underrepresented. We also present a variation of the technique where the distribution is skewed in a limited and predictable way, potentially increasing the performance. Experimental evaluation of the techniques shows that the uniform derived generators are much easier to define than hand-written ones, and their performance, while lower, is adequate for some realistic applications.

Can we solve this through engineering?

Theses for the Directer of Director of Parlosorney Random Structured Test Data Generation for Black-Box Testing

MICHAŁ H. PAŁKA

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CHALMERS | GÖTEBORG UNIVERSITY



Department of Computer Science and Engineering CHALMERS UNIVERSITY OF TECHNOLOGY AND GÖTEBORG UNIVERSITY Göteborg, Sweden 2014

THESIS FOR THE DECREE OF DOCTOR OF PHILOSOPHY

Automating Black-Box Property Based Testing

Jonas Duregård

CHALMERS | GÖTEBORG UNIVERSITY



Department of Computer Science and Engineering Chalmers University of Technology and Göteborg University Göteborg, Sweden 2016

So what is their trick?

Bag of tricks

- I. some gross stuff to ensure sharing (implemented in the size-based package)
- 2. some DSL magic for building enumerations (implemented in the testing-feat package)
- 3. some gross stuff to filter ill-typed terms eagerly (implemented in the lazy-search package)

QuickCheck, some programs please?

"There is no generic arbitrary implementation included because we don't know how to make a high-quality one. If you want one, consider using the testing-feat or generic-random packages."

- xoxo QuickCheck

Gross stuff to ensure sharing

(hint: it's encapsulated global mutable state)

DSL magic for building enumerations

```
instance Enumerable Z where
enumerate = datatype [] -- a blatant truth
instance Enumerable n => Enumerable (S n) where
enumerate = datatype [ v0 FZ , v1 FS ]
```

```
instance Enumerable Type where
enumerate = datatype [ v0 Void , v2 (:->) ]
```

```
instance Enumerable n => Enumerable (Term n) where
enumerate = datatype [ pay (v1 Var) , pay (v1 Lam) , pay (v3 App) ]
```

Does it work out of the box?

-- get me all programs of size <30
\$ eleanor --system Untyped --action Print --size 30
[Lam (Var FZ), Lam (Lam (Var FZ)), Lam (Lam (Var (FS (FZ)))), ...]</pre>

-- how many programs of size <30?
\$ eleanor --system Untyped --action Count --size 30
7964948391145</pre>

-- how many programs of size <100?
\$ eleanor --system Untyped --action Count --size 100
4503787720194931500936021688288566428450647198899831131920</pre>

Does it work out of the box?

-- how many programs of size <1000?</p>

\$ eleanor --system Untyped --size 1000

 $308979047539797286389554754656050850905240507708427967498701817852887971931069975365901\\857378119631500575402859069294978611884417142648912870521418834178736010885629562442174\\695729552893817244891920582785029398882622008238200608644806387090253102487903461107900\\446985363433164099802667368836306482954336643903824771835185388183129889962918463489147\\669085392503510337274432408608493215807279736697555590998870222330656848190305130272295\\748823658429313198623977474018608312268715019965824283441864212858719037406270777784320\\128035445486523339972120044617149804509803809721945756672127484790222562203093028297330\\701810553080361603375463934103265024019533365037819232420615636268119286995638542364078\\581194561105664479452966258068391627683565675385447131617537498143916191855677543179164\\38424355480696688647214814359468956803017461383159776132586$

real 1m 26.740s user 1m 23.087s sys 0m 1.216s

Gross stuff to filter ill-typed terms eagerly

univ :: (a -> Bool) -> (b -> a) -> Maybe Bool
univ pred val = unsafePerformIO \$
 Just (pred (val undefined)) `catch` \err -> Nothing

-- will this program ever be well-typed?
> univ (check [] Void) (\hole -> Lam hole)
Just False -- no

-- will this program ever be well-typed?
> univ (check [] (Void :-> Void)) (\hole -> Lam hole)
Nothing -- dunno?

Gross stuff to filter ill-typed terms eagerly

univ :: (a -> Bool) -> (b -> a) -> Maybe Bol () prod al - unsafePerform () univ () univ () (a -> a) -> Maybe Bol () prod al - unsafePerform () ca ch () (rr - Ucb U) -- will this regram evel be wellDtyped? Drack II Cia (noce-> I Shole a Oer -- will this program ever be well-typed? > univ (check [] (Void :-> Void)) (\hole -> Lam hole)

Nothing -- dunno?

Does it work out of the box?

-- get me the programs of type `Void :-> Void` and size <30!
\$ eleanor --system SimplyTyped --action Print --size 30
[Lam (Var FZ), Lam (App (Lam (Var FZ)) (Var FZ) Void), ...]</pre>

-- how many programs of type `Void :-> Void` and size <30?
\$ eleanor --system SimplyTyped --action Count --size 30
11369362</pre>

- real 6m 31.701s -- does not look as good
- user 6m 25.991s -- slower by a magnitude
- sys Om 3.950s -- but better than anything I've written

Problem solved!

I made a lie fi

This is linear¹

⁽i.e. variables must be used exactly once)

This is affine²

```
let s = fork!(move |s: Send<(), End>| {
    let s = send((), s)?;
    close(s)
});
let ((), s) = recv(s)?;
close(s)
```

²(i.e. variables can be used at most once)

This is neither³

```
data Type
   = Void
   | Type :-> Type
data Term n
   = Var n
   | Lam (Term (S n))
   | App (Term n) (Term n) Type -- this isn't new anymore
check :: [Type] -> Type -> Term n -> Bool
check env a (Var n) = lookup env n == a
check env (a : -> b) (Lam t) = check (a : env) b t
check env b (App f s a) = check env (a :-> b) f \& check env a s
                 _ = False
check _ _
```

³ (i.e. variables can do whatever they want! 😱)







Generate programs, then take the linear ones!

What proportion of all programs is linear?

Universal Logic Corner

How big is BCI fragment of BCK logic

KATARZYNA GRYGIEL, PAWEł M. IDZIAK and MAREK ZAIONC

Department of Theoretical Computer Science, Faculty of Mathematics and Computer Science, Jagiellonian University, Łojasiewicza 6, 30-348 Kraków, Poland.

E-mail: grygiel@tcs.uj.edu.pl; idziak@tcs.uj.edu.pl; zaionc@tcs.uj.edu.pl

Abstract

We investigate quantitative properties of BCl and BCK logics. The first part of the article compares the number of formulas provable in BCl versus BCK logics. We consider formulas outlit on implication and a fixed set of k variables. We investigate the proportion between the number of such formulas of a given length n provable in BCl logic against the number of formulas of length n provable in richer BCK logic. We examine an asymptotic behaviour of this fraction when length n of formulas tends to infinity. This limit gives a probability measure that randomly chosen BCK formula is also provable in BCl. We prove that this probability tends to zero as the number of variables tends to infinity. The second part of the article is devoted to the number of lambda terms representing proofs of BCl and BCK logics. We build a proportion between number of such proofs of the same length n and we investigate asymptotic behaviour of this proportion when length of proofs tends to infinity. We demonstrate that with probability 0 a randomly chosen BCK proof is also a proof of a BCl formula.

Keywords: BCK and BCI logics, asymptotic probability in logic, analytic combinatorics.

What proportion of affine programs is linear?

"Theorem 42. The density of BCI terms among BCK terms equals 0." — xoxo Grygiel, Idiziak, and Zaionc



Can we solve this through engineering?

"Sometimes you just have to be stupid and try to search an immensely huge search space just 'cuz you can."

- xoxo some A.I. researcher (probably)

l tried

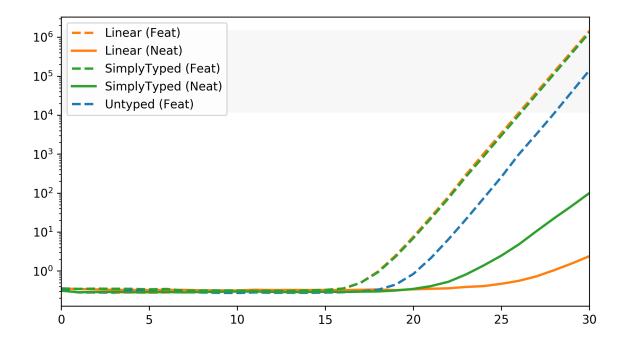
```
check :: Fin => Type -> Term n -> State (Map n Type) Bool
check a (Var x) = do
   env <- get
                                          -- . . .
   modify (delete x)
                                       -- remove variable
   return $ lookup FZ env == Just a -- was the type right?
check (a :-> b) (Lam t) = do
    modify (insert FS a . mapKeys FS) -- insert new variable
   cond1 <- check a t
                                          -- check body
   env <- get
                                          -- . . .
   let cond2 = lookup FZ env == Nothing -- was new variable used?
   modify (mapKeys pred)
                                          -- restore old variables
    return $ cond1 && cond2
check b (App f s a) = do
    cond1 <- check (a :-> b) f
                                        -- check function
   cond2 \leftarrow check a s
                                          -- check argument
   return $ cond1 && cond2
check _ _ = do return False
```

(That's too much code, Wen! 😨)

I tried, it's pretty good, actually...

-- how many linear programs of type `Void :-> Void` and size <30?
\$ eleanor --system Linear --action Count --size 30
9790</pre>

real 0m 2.580s user 0m 2.361s sys 0m 0.264s



TESTING RUSTY VARIATION

(x) generate random EGV term

- () compile EGV train to Rust
 () run Rust term and 1/2 train
 () check trace with EGV term

Where were we?

HOW EFFICIENT IS RUSTY VARIATION?

- » buffers are either empty or non-empty
- » size of buffers is statically known
 (unless you're sending boxed references)
- » each buffer only involves a single allocation
- » size of session is statically known

(but buffers are allocated lazily)

» <u>it's really quite efficient y'all</u>



session-types

- (by Laumann et al.)
- » library for session types in Rust
- » dibsed the best package name
- » embeds LAST² in Rust
 - (a linear language embedded in an affine one)
- » forget to complete a session? segfault!

 $^{\rm 2}$ Linear type theory for asynchronous session types, Gay & Vasconcelos, 2010

CONCLUSIONS

RUSTY VARIATION

- » embeds EGV into Rust
- » is unit tested
- » will be QuickChecked
- » is very efficient
- » improves session-types

